

## Subject Information Guide

### Topological Groups MATH4102

**Semester 2, 2015**

#### Administration and contact details

<b>Host Department</b>	School of Mathematical and Physical Sciences
<b>Host Institution</b>	The University of Newcastle
<b>Name of lecturer</b>	Colin Reid
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#### Subject details

<b>Handbook entry URL</b>	<a href="http://www.newcastle.edu.au/degrees/bachelor-of-mathematics-honours/handbook">http://www.newcastle.edu.au/degrees/bachelor-of-mathematics-honours/handbook</a>
<b>Subject homepage URL</b>	<a href="http://www.newcastle.edu.au/course/MATH4102">http://www.newcastle.edu.au/course/MATH4102</a>
<b>Honours student hand-out URL</b>	To be advised
<b>Start date:</b>	Monday 27 July 2015
<b>End date:</b>	Friday 6 November 2015
<b>Contact hours per week:</b>	3 (2 hours lecture, 1 hour tutorial)
<b>Lecture day and time:</b>	To be determined
<b>Description of electronic access arrangements for students (for example, WebCT)</b>	Notes, exercises and assignments will be emailed to students. Assignments are submitted as pdf's and returned with annotations.

#### Subject content

##### 1. Subject content description

An introduction to the theory of topological, and in particular locally compact, groups. The fundamental theorems will be explained and proved in special cases.

## Course content

### 2. Week-by-week topic overview

The course will aim to cover the following topics. There may be some variation depending on the interests and backgrounds of students.

#### Weeks 1–2 General topological groups

- (a) Definitions and notation, derivation of basic properties.
- (b) Compact and locally compact groups.
- (c) Subgroups, quotients by closed normal subgroups. Products of groups.
- (d) Connected and totally disconnected groups.

Examples, many of which will be referred to throughout the course, are discussed in exercises and the first assignment.

#### Weeks 2–4 The Haar integral

- (a) Existence and uniqueness of a left translation-invariant integral.
- (b) The modular function. Unimodular groups.
- (c) Proof of existence on compact groups.

Examples of explicit Haar integrals on particular groups will be given in lectures and exercises. Further examples on connected and totally disconnected groups seen later.

#### Weeks 5–8 Totally disconnected groups

- (a) Compact open subgroups.
- (b) Totally disconnected locally compact fields.
- (c) Haar measure.
- (d) The scale and minimizing subgroups for automorphisms.

(e) Flat groups of automorphisms.

(f) Applications and particular classes of totally disconnected groups.

#### Weeks 9–12 Connected groups

(a) Lie groups and matrix groups.

(b) Connected locally compact fields.

(c) Approximation by Lie groups. Hilbert's 5th problem.

(d) Compact connected groups.

(e) Haar measure on some connected matrix groups.

(f) Some consequences of approximation by Lie groups.

### **3. Assumed prerequisite knowledge and capabilities**

(1) Point set topology or the metric spaces.

MATH3180 Topology <http://www.newcastle.edu.au/course/MATH3180.html>

(2) Groups, rings and fields.

MATH3120 Algebra <http://www.newcastle.edu.au/course/MATH3120.html>

(3) Linear Algebra.

MATH2320 Linear Algebra <http://www.newcastle.edu.au/course/MATH2320.html>

(4) Some combinatorics (graph theory) and number theory (modular arithmetic) would also be useful.

### **4. Learning outcomes and objectives**

1. Demonstrate an understanding of the content and context of an advanced mathematical topic;

2. Apply advanced mathematical problem solving skills

3. Use sophisticated mathematical communication skills in the presentation of mathematical arguments

## 5. Learning resources

Notes and exercises provided.

## 6. Assessment

Exam/assignment/classwork breakdown					
<b>Exam</b>	60 %	<b>Assignment</b>	35 %	<b>Class work</b>	5%
<b>Assignment due dates</b>		To be advised			
<b>Approximate exam date</b>				Tuesday 9 June – Friday 26 June 2015	

## Institution Honours program details

<b>Weight of subject in total honours assessment at host department</b>	Course is 10 units from a total of 80 units for the Honours year.
<b>Thesis/subject split at host department</b>	50 units for courses and 30 units for thesis.
<b>Honours grade ranges at host department:</b>	
<b>H1</b>	85-100 %
<b>H2a</b>	75-84 %
<b>H2b</b>	65-74 %
<b>H3</b>	50-63 %